

**TIE-50406 DSP Implementations**

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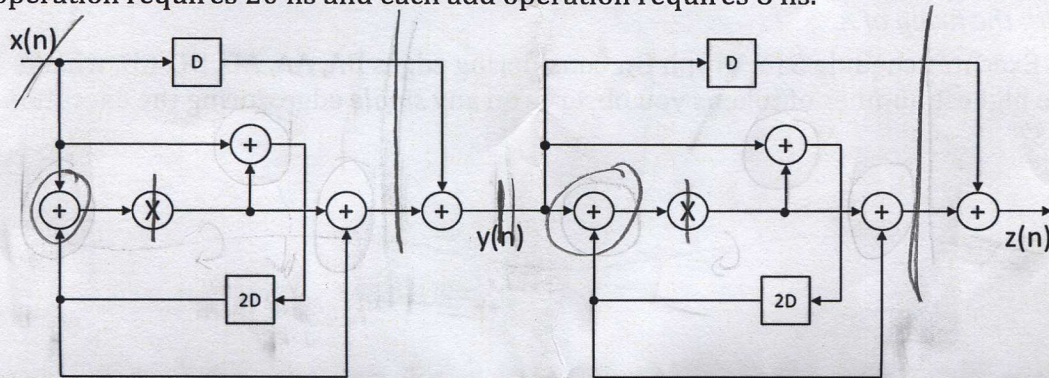
Exam Dec. 15, 2016

**Calculators and dictionaries are allowed**

1. Explain shortly:

- a) recursive DFG
- b) M-level pipelined system
- c) Biased exponent
- d) SDFG
- e) L-slow
- f) precedence constraint in data flow graphs

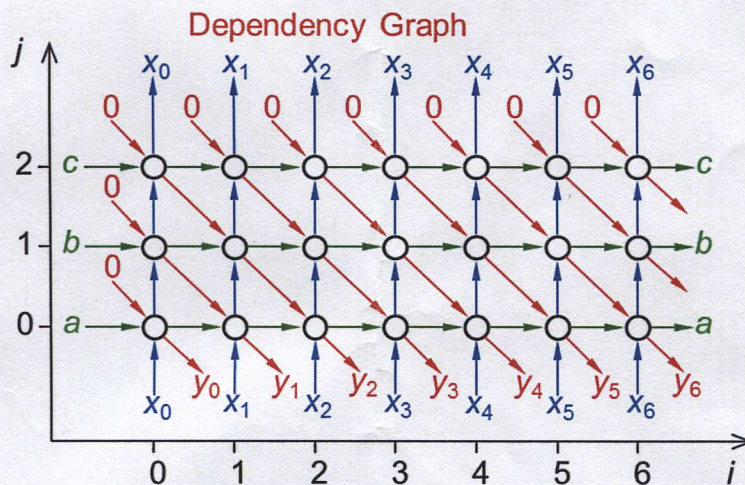
2. Consider the wave digital filter shown below. Assume that each multiply operation requires 20 ns and each add operation requires 8 ns.



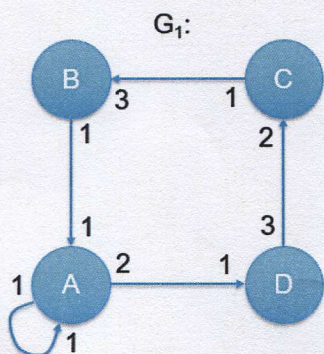
- a) Calculate the iteration bound of this filter by inspection.
- b) What is the critical path?
- c) Manually pipeline and/or retime this filter to achieve a critical path equal to the iteration bound.

3. Draw the systolic architecture block diagram and the space-time mapping for the 3-tap FIR digital filter (dependence graph below) with the projection, processor, and scheduling vectors as follows:

$$\mathbf{d} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}, \quad \mathbf{p}^T = (1 \quad 1), \quad \mathbf{s}^T = (2 \quad 1).$$



4. Consider the synchronous dataflow graph  $G_1$  below:



- a) Determine the topology matrix  $\Gamma$  of  $G_1$
- b) Acquire the repetition vector  $\mathbf{q}$  by solving  $\Gamma \mathbf{q}^T = \mathbf{0}$  or by balance equations.
- c) Construct a valid and periodic sequential schedule  $S$  for  $G_1$ . For  $S$  to be periodic, which edge(s) need initial tokens, and how many of them? *Make your schedule start with the firing of A.*
- d) Execute schedule  $S$  for graph  $G_1$ . Considering edges BA, AA, AD, DC, CD, what is the highest number of tokens you observe on any *single* edge during the execution of  $S$ ?